Abstract: We consider the problem of sorting a set of items having an unknown total order by doing binary comparisons of the items, given the outcomes of some pre-existing comparisons. We present a simple algorithm with a running time of $O(m + n + \log T)$, where $n$, $m$, and $T$ are the number of items, the number of pre-existing comparisons, and the number of total orders consistent with the outcomes of the pre-existing comparisons, respectively. The algorithm does $O(\log T)$ comparisons.

Both our time and comparison bounds are best possible up to constant factors, thus resolving a problem which has been open since 1978 (Fredman, Theoretical Computer Science). The best previous algorithm with a bound of $O(\log T)$ on the number of comparisons has a non-linear time bound and is much more complicated. Our algorithm combines two classic algorithms: topological sort and heapsort, with the right kind of heap.

This is joint work with Bernhard Haeupler, Richard Hladík, John Iacono, Václav Rozhoň, and Jakub Tětek.

Bio: Robert E. Tarjan is the James S. McDonnell Distinguished University Professor of Computer Science at Princeton University. He has held academic positions at Cornell, Berkeley, Stanford, and NYU, and industrial research positions at Bell Labs, NEC, HP, Microsoft, and Intertrust Technologies. He has invented or co-invented many of the most efficient known data structures and graph algorithms. He was awarded the first Nevanlinna Prize from the International Mathematical Union in 1982 for “for outstanding contributions to mathematical aspects of information science,” the Turing Award in 1986 with John Hopcroft for “fundamental achievements in the design and analysis of algorithms and data structures,” and the Paris Kanellakis Award in Theory and Practice in 1999 with Daniel Sleator for the invention of splay trees. He is a member of the U.S. National Academy of Sciences, the U. S. National Academy of Engineering, the American Academy of Arts and Sciences, and the American Philosophical Society. He has published more than 200 papers in high-quality refereed journals, more than 100 papers in refereed conference proceedings, and holds 38 U.S. Patents.

For more info: Please contact vozirani@ics.uci.edu